

# ITRF Transformations in Deforming Zones to Support CORS-NRTK Applications

**Never Stand Still** 

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# NRTK in deforming zones – The problem

NRTK requires high precision CORS coordinates (LU < 15 mm) in order to correctly model biases (e.g. troposheric, ionospheric) and orbit errors

Only achievable in tectonically active regions if near real-time (kinematic or dynamic) ITRF or IGS reference frame used for CORS.

#### BUT

#### Kinematic ITRF isn't a practical working datum for NRTK users

Very difficult to harmoniously integrate surveys done at different times (e.g. engineering surveys, cadastral/DCDB, 3D laser scans, LiDAR, GIS)

e.g. between 700 mm difference between 2002 and 2012 due to movement of Australian tectonic plate

The classic "Standard rail gauge / train wreck problem"





# NRTK in deforming zones – A solution

# Kinematic (dynamic) ITRF and IGS RF coordinates can be transformed to a working "static" geodetic datum using a robust deformation model

Best of both worlds: The complexity of global and local deformation modelling is handled by the NRTK server and software. End users do not "see" changes





# Rigid plate deformation of CORS-NRTK



ement  

$$\begin{bmatrix} \mathbf{i} \\ X \\ \mathbf{i} \\ Y \\ \mathbf{i} \\ \mathbf{i} \\ \mathbf{i} \\ \mathbf{i} \end{bmatrix} = \begin{bmatrix} \Omega_Y Z - \Omega_Z Y \\ \Omega_Z X - \Omega_X Z \\ \Omega_X Y - \Omega_Y X \end{bmatrix} \bullet 1 \text{E-6}$$

Velocity and position can be estimated from rigid plate model  $(\Omega_X, \Omega_Y, \Omega_Z)$ 

or by 14 parameter transformation



# **Coseismic offsets and Coordinate Changes**



coordinate changes (seismic patch model) to reflect visible reality – an inconvenient truth.



# Deformation modelling from time-series analysis





# Deformation modelling pathways





### Nested data structure for deformation models





#### Deformation model in practice

$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{t_0} = \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{t} + \begin{bmatrix} X \\ X \\ Y \\ Z \end{bmatrix} \bullet (t_0 - t) - \begin{bmatrix} \Delta X \\ \Delta Y \\ \Delta Z \end{bmatrix}_{PATCH}$$

<i>t</i> <sub>0</sub>	is the reference epoch (in decimal years)
t	is the epoch of measurement (in decimal years)
$(X, Y, Z)t_0$	are the coordinates computed at the reference epoch (metres),
(X, Y, Z)t	are the kinematic ITRF coordinates at the measurement epoch (in metres),
(X,Y,Z)	is the ITRF site velocity interpolated from the interseismic velocity model (m/yr),
$(\Delta X, \Delta Y, \Delta Z)_{PATCH}$	is the accumulated seismic deformation between the reference and measurement epochs interpolated from the most up-to-date seismic patch model (in metres)



### New Zealand Case Study





#### Slow-slip event deformation





# Separating seismic and interseismic deformation from time-series

Seismic patch is a sum of all non-linear (episodic) deformation between reference and measurement epoch





# Localised deformation model components





#### Example

Rover (PRTU) ITRF2008 Epoch 2011.008

S 38 48' 51.0946" E 177 41' 52.3646"

The ITRF site velocity from interseismic velocity model : E -0.0108 m/yr N 0.0217 m/yr The seismic patch model at epoch 2011.0  $\Delta E \ 0.183 \text{ m} \quad \Delta N \ 0.008 \text{ m}$ NZGD2000 (estimated from model) S 38 48' 51.1026" E 177 41' 52.3620" NZGD2000 (tabulated) S 38 48' 51.1021" E 177 41' 52.3619"

**Tabulated – estimated:** 

ΔE -0.002 m ΔN 0.014 m



# Conclusions

NRTK should account for reference frame deformation (LU < 15 mm)

NRTK optimally uses latest IGS weekly or daily solution (IGS rapid orbit)

A composite deformation model transforms coordinates between kinematic (dynamic) ITRF/IGS and a static/semi-kinematic datum

- 1. interseismic velocity model to account for larger and linear plate motion
- 2. seismic patch model to account for seismic deformation and other distortions

NRTK on rigid plates can use rigid plate rotation model or 14 parameter transformation

NZ Case study shows how concept and application can work in practice

#### **Benefits:**

Increased longevity of a working static / semi-kinematic geodetic datum

Complexity of global and local deformations handled at NRTK server or software level

End users do not "see" coordinate changes unless a large earthquake has occurred.

